

37.25. Model: Use the relativistic expression for the total energy.

Solve: (a) The energy of the proton is

$$E = \gamma_p mc^2 = \frac{1}{\sqrt{1 - v^2/c^2}} mc^2 = \frac{1}{\sqrt{1 - (0.99)^2}} mc^2 = (7.089)(1.67 \times 10^{-27} \text{ kg})(3.0 \times 10^8 \text{ m/s})^2$$
$$= 1.065 \times 10^{-9} \text{ J} \times \frac{1 \text{ eV}}{1.6 \times 10^{-19} \text{ J}} = 6.66 \times 10^9 \text{ eV} = 6.66 \text{ GeV}$$

(b) Likewise, the energy of the electron is

$$E = \frac{1}{\sqrt{1 - (0.99)^2}} (9.11 \times 10^{-31} \text{ kg})(3.0 \times 10^8 \text{ m/s})^2 = 5.812 \times 10^{-13} \text{ J} \times \frac{1 \text{ eV}}{1.6 \times 10^{-19} \text{ J}} = 3.63 \times 10^6 \text{ eV} = 3.63 \text{ MeV}$$

Assess: The total energy E for the proton is larger than that for the electron by the factor $m_{\text{proton}}/m_{\text{electron}} = 1833$.